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2.5	43-49
2.6	50-50
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3.2.	61-68
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4.1		69-69
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4.3.		80-88
4.4.		88-89
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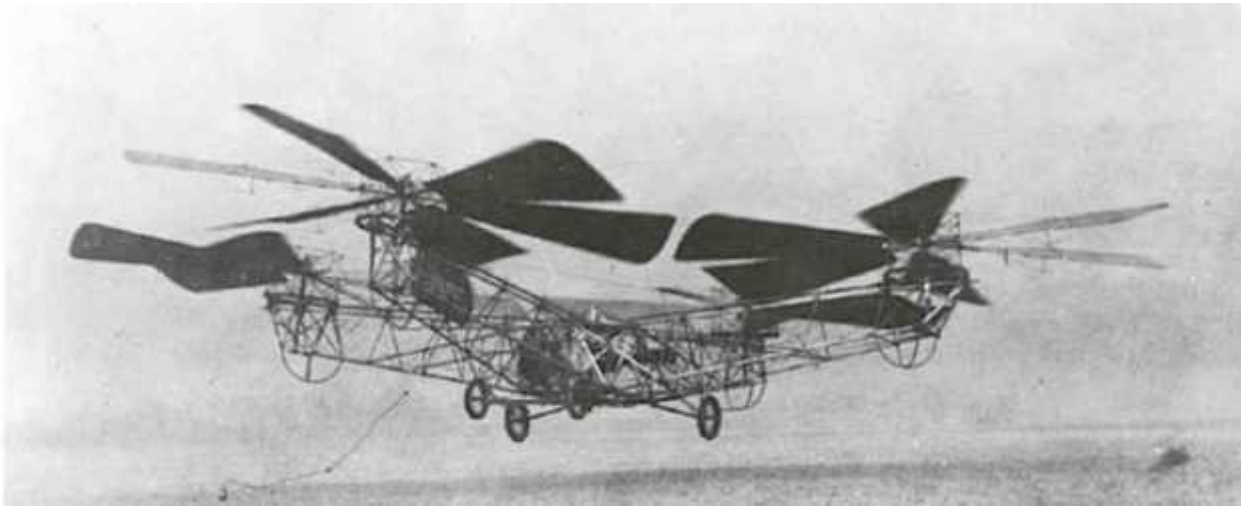
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Global Hawk () Heron (), Predator, Reaper,

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2023 , Parrot
Bebop Drone 2, Xiro XPLOER V, Autel Robotics X-Star Premium, Xiaomi Mi Drone
4 , YUNEEC Typhoon Q500 4K, DJI Phantom 3 SE, DJI Spark, DJI Mavic Air, DJI
Mavic Pro YUNEEC Typhoon H.

Parrot Bebop Drone 2:

: Parrot Bebop Drone 2

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Xiro XPLOER V:

: Xiro XPLOER V – , -

: GPS- , ,

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Autel Robotics X-Star Premium:

: Autel Robotics X-Star Premium – ,

: 4K Ultra HD , 12 , GPS- ,

: - ,

Xiaomi Mi Drone 4K:

: Xiaomi Mi Drone 4K –

: 4K, ,

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YUNEEC Typhoon Q500 4K:

: YUNEEC Typhoon Q500 4K – ,

: 4K Ultra HD , 12 , GPS, Smart Mode

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DJI Phantom 3 SE:

[] : DJI Phantom 3 SE –

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, 4K , GPS,

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DJI Spark:

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, LQR- PID - , (SOF) ().

(MILS)

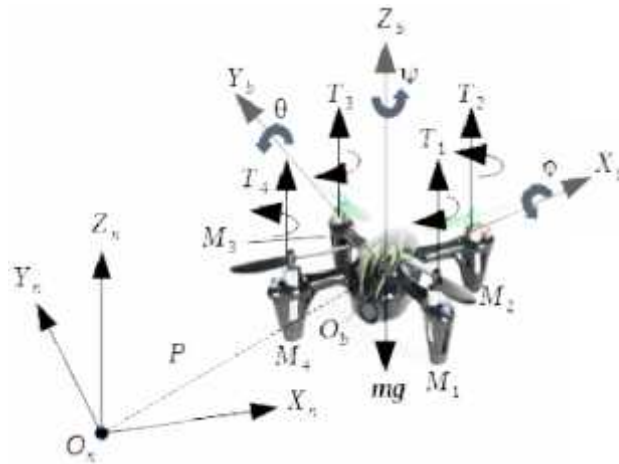
MILS

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T_z -
 θ

$$T_z = \sum_{i=1}^4 T_i.$$

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M_4

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M_2 .

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M_1, M_2 .

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M_1

M_3

()

M_2, M_4 .

T_z

4-

T_z

$$P = [p_x, p_y, p_z] -$$

(O_D ,

.1)

()

$O_n X_n Y_n Z_n \phi, \theta, \psi$, -

, T_i - , $i - th$
 $M_i (i = 1, \dots, 4)$. $O_D X_D Y_D Z_D$ - .

:

$$m_Q \ddot{P} = \mathfrak{R}T,$$

$$J\ddot{\theta} = C(J, \theta, \dot{\theta}) + Q, \quad (1.1)$$

:

m_Q -

\mathfrak{R} - (DCM)

T - , J -

$\theta = [\phi, \theta, \psi]$ -

$C(J, \theta, \dot{\theta})$ -

Q - , .

(1.1) ,

, . (1.1)

, $P i \theta$,

(1.1)

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X- , X

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Y - , Y
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 Z - , Z ;
 ψ - , Z .

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$$\frac{d}{dt}(t) = A_x(t) + B_u U(t) + B_d D(t),$$

$$v(t) = C_x(t), \quad (1.2)$$

$x(t)$ -

$U(t)$ -

$D(t)$ - ()

$v(t)$ -

A -

B_u -

B_d -

C -

(2)

(1.1)

(1.2),

(1.1)

:

$$\chi = [p_x, \dot{p}_x, p_y, \dot{p}_y, p_z, \dot{p}_z, \phi, \dot{\phi}, \theta, \dot{\theta}, \psi, \dot{\psi}]. \quad (1.3)$$

$$M_i (i = 1, \dots, 4),$$

),

(
LQR,

LQR

X-

$$\frac{d^2 p_x}{dt^2} = -g \frac{\sin \theta}{\cos \phi}, \quad (1.4)$$

$$J_x \frac{d^2 \theta}{dt^2} = Q_\theta, \quad (1.5)$$

Y-

$$\frac{d^2 p_y}{dt^2} = g \tan \phi, \quad (1.6)$$

$$J_y \frac{d^2 \phi}{dt^2} = Q_\phi, \quad (1.7)$$

Z-

$$\frac{d^2 p_z}{dt^2} = \frac{T_z}{m_Q} \cos \phi \cos \theta - g, \quad (1.8)$$

$$J_z \frac{d^2 \psi}{dt^2} = Q_\psi, \quad (1.9)$$

(1.3) - (8) g - 9,81 / , T_z -

$$4- : Y_z = \sum_{i=1}^4 T_i \cdot Q_\theta, Q_\phi, Q_\psi - , (1).$$

ϕ, θ, ψ

$$(\tan \phi \approx \phi, \cos \phi \approx 1) \quad (1.2)$$

(1.4) - (1.9)

T_i

Q_i ,

$$: T_i = K_i \omega_i^2 \quad Q_i = K_Q \omega_i^2, \quad K_T, K_Q -$$

K_Q K_T

$$W_e(s) = \frac{K_e}{\tau_e s + 1}, \quad (1.10)$$

K_e τ_e - ($I(t)$)
 $\Omega(t)$)

4

Ω_0

$$:T_z = m_Q g$$

Y (. .1.4) : $\Omega_2 = \Omega_0 + \Delta\Omega_2, \Omega_4 = \Omega_0 - \Delta\Omega_2.$,

$\Delta\Omega_i$

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2.1

2.2.

2.1

:

$$\begin{cases} \frac{d}{dt}(t) = A_{\chi}(t) + B_u u(t) + B_d(t)d(t); \\ v(t) = C_{\chi}(t), \end{cases} \quad (2.1)$$

A, B_u, B_d

:

$$\chi = [\chi_1, \chi_2, \chi_3, \chi_4, \chi_5]^T = [y, d/d, \varphi, d/d, \Omega]^T, \quad (2.2)$$

$y -$

$Y, d/d -$

$\varphi, d/d -$

$, \Omega -$

$, d(t) -$

(

$), u -$

.

A, B_u, B_d, C

(,).

:

$$m_Q = 5,5$$

Foxtech X5010 KV288 $m =$

0,213 ;

$$l = 0,343$$

2.1,

1- 2- 1-
1- :

$$W_e(s) = \frac{K}{\tau_e s + 1}, \quad (2.3)$$

K - ,
 τ_e - .
(u),
(ESC), -
 Ω , ,
X 2- (1).

A, B_u, B_d, C , (1) 2.1,

$$A = \begin{bmatrix} 0 & 1 & 0 & 0 & 0 \\ 0 & -0.28 & 9.81 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 13.51 \\ 0 & 0 & 0 & 0 & -8.33 \end{bmatrix},$$

$$B_u = \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 10.42 \end{bmatrix}, B_d = \begin{bmatrix} 0 \\ 1 \\ 0.0285 \\ 0 \\ 0 \end{bmatrix}, A = \begin{bmatrix} 1 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \end{bmatrix}. \quad (2.4)$$

2.3

),
 K (
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):

$$u(t) = +K(t) = -KC_x(t), \quad (2.5)$$

:
 $K \in R^{1 \times 4}, C \in R^{4 \times 5}$,
 $d(t)$

L_2 -

$$J = \int_0^{\infty} z(t)^2 dt = \int_0^{\infty} (x^T Q + u^T R) dx. \quad (2.6)$$

$$z = \begin{bmatrix} \sqrt{Q} & 0 \\ 0 & \bar{R} \end{bmatrix} \begin{bmatrix} x \\ u \end{bmatrix}, \quad (2.7)$$

:

$$\frac{\int_0^{\infty} z(t)^2 dt}{\int_0^{\infty} d(t)^2 dt} = \frac{\int_0^{\infty} (x^T Q + u^T R) dx}{\int_0^{\infty} (d^T d) dx} \gamma^2 \quad (2.8)$$

, () $F \in R^{1 \times 4}$, (8).

, γ γ .

H_∞ , :"
 $Q = 0$, $(A, Q^{\frac{1}{2}})$, (A, B_u) ,
 $\gamma > \gamma$. SOF K ,
 $A_0 = (A - B_u K)$
 L_2 , , L ,

$$K = R^{-1}(B_u^T P + L), \quad (2.9)$$

$$P = P^T \geq 0, \quad ,$$

():

$$P + A^T P + Q + \frac{1}{\gamma^2} P B_d B_d^T P - P B_u R^{-1} B_u^T P + L^T R^{-1} L = 0. \quad (2.10)$$

$H_\xi(s)$ - d
 z , $\|H_\xi(s)\|_\infty < \gamma$.
 H_∞ - .
 , .
 , (10).

2.4

H -

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, (10):

$$\begin{bmatrix} P + A^T P + Q & P B_u & P B_d & L^T \\ & B_u^T P & -R & 0 \\ & B_d^T & 0 & -\gamma^2 I \\ & L & 0 & -R \end{bmatrix} < 0. \quad (2.11)$$

ARE (2.10) LMI (2.11)

(2.8)

(2.11). (2.11)

MATLAB.

H_∞ $d(t)$

H_∞

2.5

1. : $n = 0, L_0 = 0, \gamma, Q, R.$

2. : P_n

$$\begin{bmatrix} P + A^T P + Q & PB_u & PB_d & L^T \\ B_u^T P & -R & 0 & 0 \\ B_d^T & 0 & -\gamma^2 I & 0 \\ L & 0 & 0 & -R \end{bmatrix} < 0.$$

3. $K: K_{n+1} = R^{-1}(B^T P_n + L_n)C^T(CC^T)^{-1}.$

4. $L: L_{n+1} = RK_{n+1}C - B^T P_n.$

5. : $K_n - K_{n+1} < \varepsilon,$

$K_{n+1} \quad K_n$

, 4,

$n = n + 1$

2.

6. : $K = K_{n+1}.$

H_∞ -SOF

(1, 4).

:

$$Q = d \ g([135 \ 210 \ 400100 \ 1000050 \ 0])$$

$$R = 2500, \gamma = 0.1, (12)$$

H_∞ -SOF: $K =$

$$[0.2324 \ 0.6244 \ 20.2750 \ 20.5419],$$

$$A = A - B \quad :$$

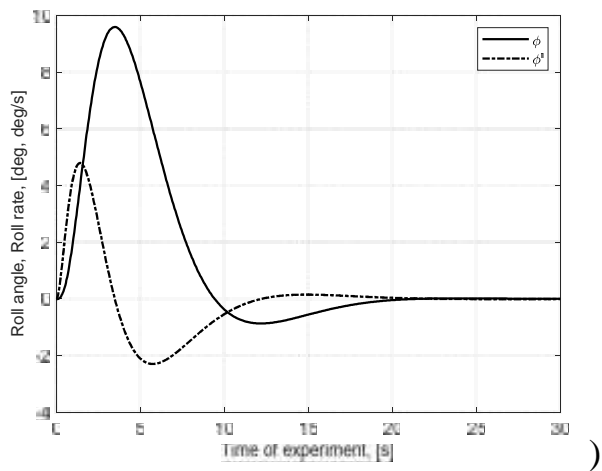
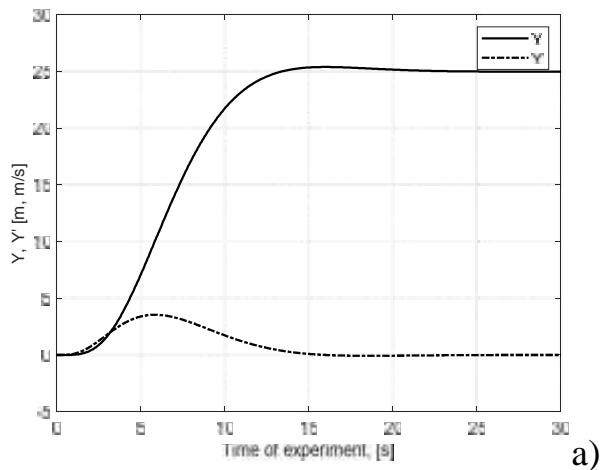
$$e \ g(A) = [-3.67 \pm 53.57i, -0.64, -0.31 \pm 0.27i].$$

$$H_\infty \quad H_\xi (s) \quad : \|H_\xi (j\omega)\|_\infty = 0.1069;$$

$$L_2 \quad \|H_\xi (j\omega)\|_2 = 0.1130.$$

$$\gamma = 0.1.$$

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. 2.1.

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$$) \chi_1 = y \quad \chi_2 = y, \quad) \chi_3 = \varphi \quad \chi_4 = \varphi$$

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2.2), - 5 / . ,

Y

X

H_{∞} -

$$K = [-0.2324 \quad -0.6244 \quad 20.2750 \quad 20.5419].$$

X Y

$$\frac{d^2x}{dt^2} = -\frac{\mu}{m_Q} \frac{d}{d} - g \frac{\tan \theta}{\cos \varphi},$$

$$\frac{d^2y}{dt^2} = -\frac{\mu}{m_Q} \frac{d}{d} - g \tan \varphi. (13)$$

.2.2

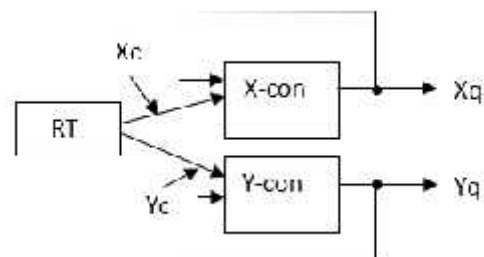
$$x - c_1 \quad y - c_1$$

X Y,

RT - ,

.2 X_c, Y_c

, X_q, Y_q -



.2.2.

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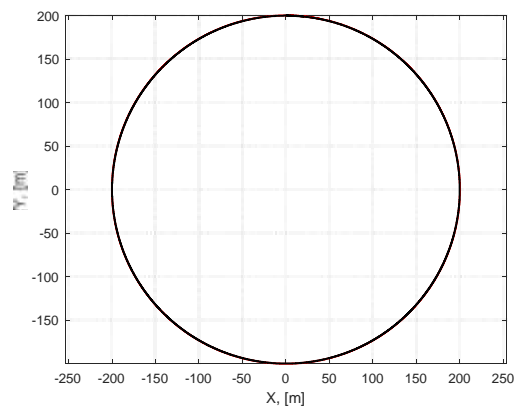
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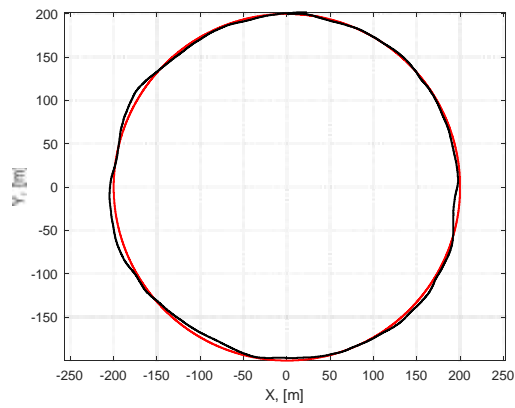
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a)

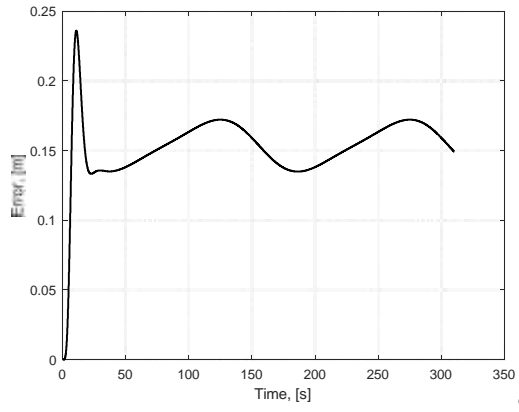


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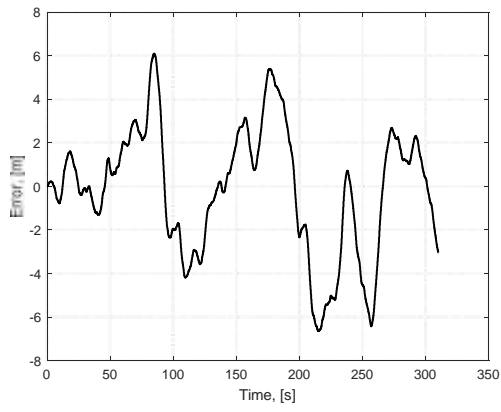
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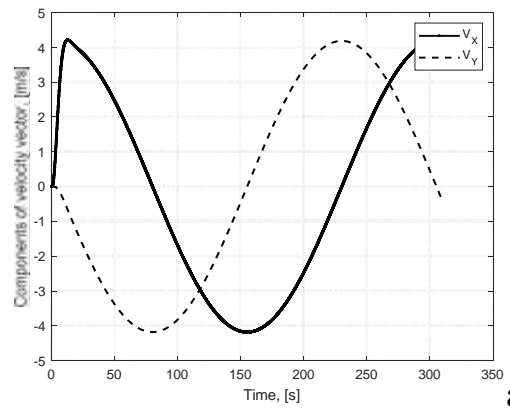


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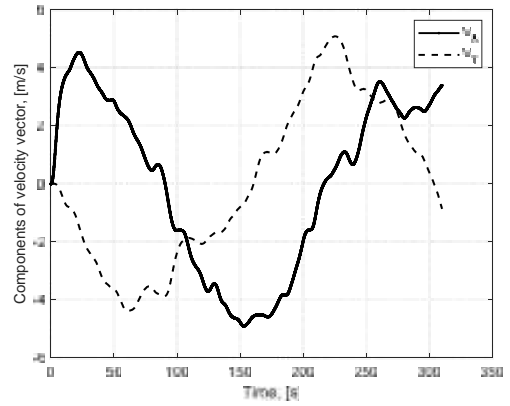
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a)

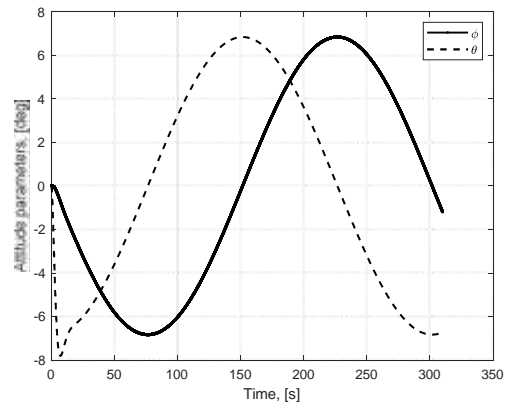


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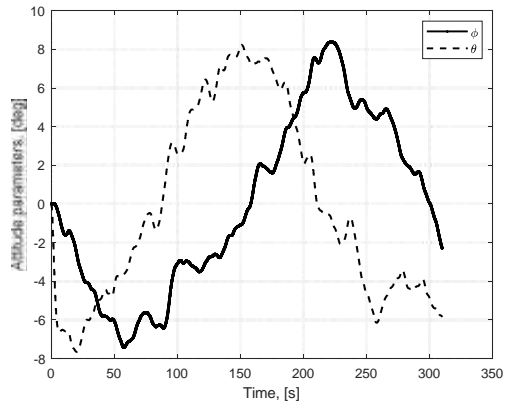
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3.1.

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, X_c, Y_c, ψ_c, Z_c -

$U_\theta, U_\phi, U_\psi, U_z$ -

ESC

$M_i (i = 1, \dots, 4)$.

Ω_1

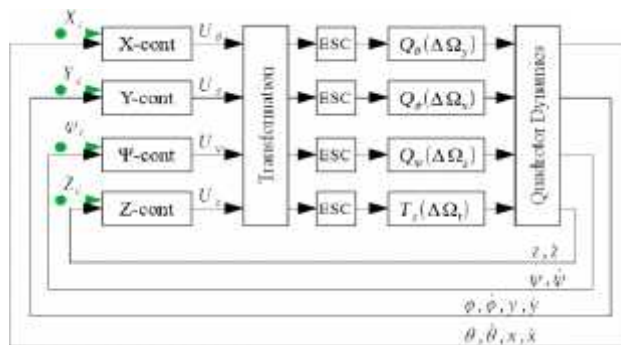
:

$$T_z = \sum_{n=1}^4 T_n = K_T \sum_{n=1}^4 \Omega_n^2 = U_z,$$

$$Q_\theta = K_T l (\Omega_2^2 - \Omega_4^2) = U_\theta,$$

$$Q_\phi = K_T l (\Omega_3^2 - \Omega_1^2) = U_\phi,$$

$$Q_\psi = K_Q [(\Omega_2^2 + \Omega_4^2) - (\Omega_3^2 + \Omega_1^2)] = U_\psi, \quad (3.1)$$



. 3.1.

$$\begin{aligned}
 & K_T - \\
 & K_Q - \\
 & l - \quad (\quad) . \quad , \quad (9)
 \end{aligned}$$

$$(4) - (7).$$

X- :

$$\frac{d^2 p_x}{dt^2} = -g\theta, \quad (3.2)$$

$$J_x \frac{d^2 \theta}{dt^2} = Q_\theta, \quad (3.3)$$

Y- :

$$\frac{d^2 p_y}{dt^2} = g\phi, \quad (3.4)$$

$$J_y \frac{d^2 \phi}{dt^2} = Q_\phi, \quad (3.5)$$

g. , Y- . :

$$\chi = [p_y, p_y, \phi, \phi]^T, \quad (3.6)$$

$$(3.2) - (3.6)$$

$$A = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & g & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 \end{bmatrix}; B_u = [0 \ 0 \ 0 \ 1]^t;$$

$$C = e \quad (4); U = Q\phi, \quad (3.7)$$

e (4) - 4×4 .

(3.7)

d_f

D .

μ ,
/ ,

d_f

$: d_f = \mu p_y,$

$d_f = \mu$

v

$: \tilde{v} = v + v_g.$

v_g

$D(t)$

(2).

$\mu_g l.$

(11)

Y-

$K_L = 4\Omega_0,$

$$(\Omega_0 + \Omega_2)^2 - (\Omega_0 - \Omega_2)^2 = 4\Omega_0 \Omega_2 \quad (3.8)$$

(3.10),

:

$$\frac{d}{dt}(t) = A_\chi(t) + B_u U(t) + B_a D(t),$$

$$v(t) = C_x(t), \quad (3.9)$$

:

$$A = \begin{bmatrix} 0 & 1 & 0 & 0 & 0 \\ 0 & -\frac{\mu}{m_Q} & g & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & \frac{K_T K_L l}{J_y} \\ 0 & 0 & 0 & 0 & -\tau_b^{-1} \end{bmatrix}$$

$$B_{ut} = \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ \frac{K_e}{\tau_e} \end{bmatrix} \quad (3.10)$$

$$B_d = \begin{bmatrix} 0 \\ 1 \\ 0 \\ -\frac{\mu}{J_y} \\ 0 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \end{bmatrix},$$

$$x = \left[p_y, v, \varphi, \frac{d}{d}, \Omega \right]^T, U(t) = I(t),$$

$$D(t) = v_g(t)$$

$$I(t) = \begin{bmatrix} 1 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \end{bmatrix}, \quad \Omega.$$

$$C = \begin{bmatrix} 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \end{bmatrix}, \quad \Omega$$

$$X = \begin{bmatrix} 1 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \end{bmatrix}, \quad (3.9)$$

$$g = \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}, \quad A = \begin{bmatrix} 0 & 1 & 0 & 0 & 0 \\ 0 & -\frac{\mu}{m_Q} & g & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & \frac{K_T K_L l}{J_y} \\ 0 & 0 & 0 & 0 & -\tau_b^{-1} \end{bmatrix} :$$

$$x = \left[p_x, u, \theta, \frac{a}{a}, \Omega \right]^T, u = p_x. \quad (3.11)$$

$$Z = \begin{bmatrix} 1 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \end{bmatrix}, \quad Z,$$

$$(9) \quad 2. \quad ,$$

$$w_g \quad \cdot \quad (3.8)$$

$$\cos \phi \cos \theta = 1, \quad 1- \quad (11) \quad (18)$$

$$T_z = m_Q g \quad :$$

$$\frac{d}{dt} \chi(t) = A \chi(t) + B_u U(t)$$

$$v(t) = C \chi(t), \quad (3.12)$$

$$A, B_u, C \quad :$$

$$A = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & \frac{8K_T \Omega_0}{m_Q} \\ 0 & 0 & -\tau_e^{-1} \end{bmatrix}, B_u = \begin{bmatrix} 0 \\ 0 \\ K_e \tau_e^{-1} \end{bmatrix}$$

$$C = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \end{bmatrix}, \chi = [p_z, w, \Omega]^T, w = p_z \quad (3.13)$$

$$- \quad (3.9),$$

$$Z, \quad :$$

$$\begin{bmatrix} \chi_1 \\ \chi_2 \\ \chi_3 \end{bmatrix} = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 8K_Q \Omega_0 J_z^{-1} \\ 0 & 0 & -\tau_e^{-1} \end{bmatrix} \cdot \begin{bmatrix} \chi_1 \\ \chi_2 \\ \chi_3 \end{bmatrix} + \begin{bmatrix} 0 \\ 0 \\ \frac{K_e}{\tau_e} \end{bmatrix}$$

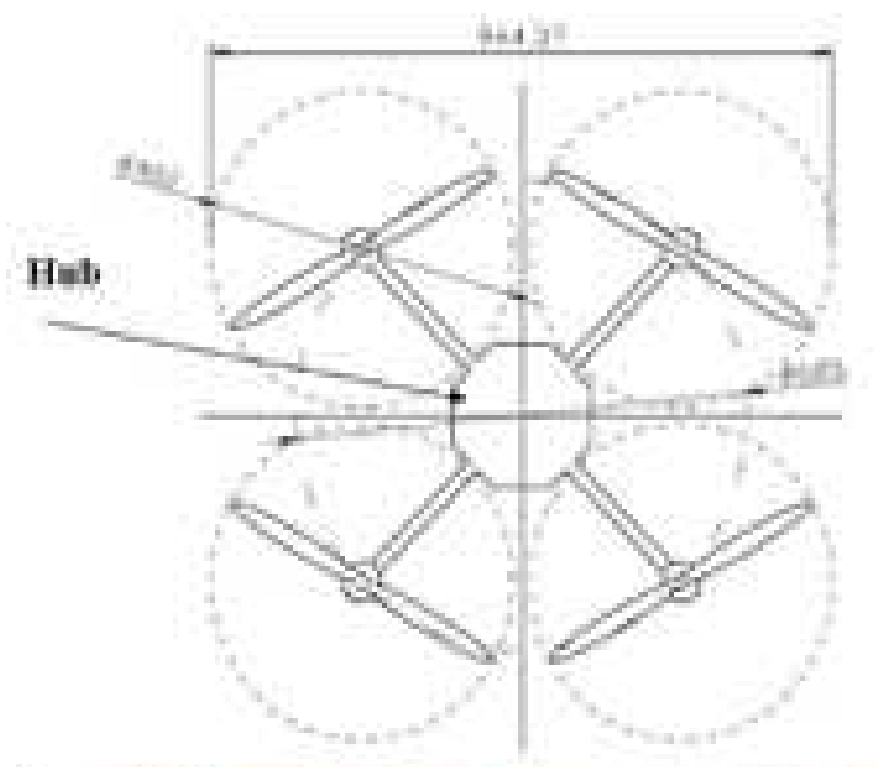
$$v(t) = C \chi(t), \chi = [\psi, \psi, \Omega]^T, U_\psi = I \quad (3.14)$$

$$C \quad (3.14), \quad (3.13).$$

$$(3.9), (3.11)$$

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"Foxtech X5010 KV288".



.3.1.

3.1

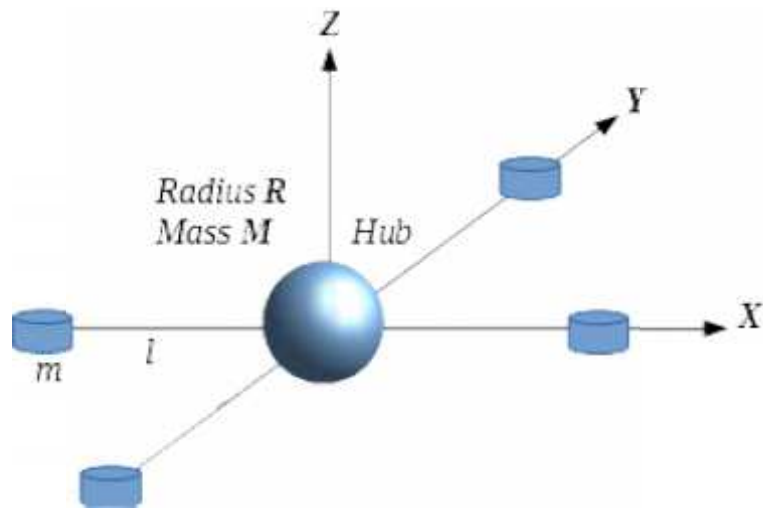
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.4, "Hub" -

3.1.

1		m_Q	5.5	
2		l	0.34	
3		M	4.65	
4		R	0.11	
5		r	0.21	
6		Ω_m	180	—
7		I_m	22.7	A
8		P_m	550	W
9		τ_e	0.12	
10.		T_m	34.3	N
			3	



. 3.2.

$m, M, l, r,$

3.1,

$$J_x = \frac{2Mr^2}{5} + 2l^2m = 0.074 [\quad ^2],$$

$$J_y = \frac{2Mr^2}{5} + 2l^2m = 0.074 [\quad ^2],$$

$$J_z = \frac{2Mr^2}{5} + 4l^2m = 0.124 [\quad ^2]. \quad (3.15)$$

(3.1) , T_i Q_i

$$: T_i = K_T \Omega_i^2, Q_i = k_Q \Omega_i^2.$$

3.1,

K_T K_Q .

:

$$K_T = \frac{T_m}{\Omega_m^2} = \frac{3,3}{(1,6)^2} = 1.05 \cdot 10^{-5} \frac{N}{m^2} \quad (3.16)$$

K_Q

$$Q = \frac{F_m}{\Omega_m} = \frac{5}{1 \cdot 6} = 0.304 \frac{W}{/} = 0,30 \quad (3.17)$$

$$P = 550 W = 550 \frac{N}{-}$$

$$K_Q = \frac{Q}{\Omega_m^2} = 9.28 \cdot 10^{-8} \frac{N}{(/)^2} \quad (3.18)$$

ESC

$$k_e = \frac{\Omega_m}{I_m} = 79.72 \frac{/}{A} \quad (3.19)$$

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$$T_{0i} = \frac{m_Q g}{4}, i = 1, \dots, 4.$$

$$\Omega_{0i} = \frac{1}{2} \sqrt{\frac{m_Q g}{K_T}} = 1133.5 \text{---} \quad (3.20)$$

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$\mu = 0,102 \text{---}$,

$m_Q = 2.75$,

$\mu = 0,77 \text{---}$.

μ , $m_Q = 5,5$
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$$\mu = 1.45 \text{ — (3.21)}$$

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(3.14) - (3.21).

Y- :

$$A = \begin{bmatrix} 0 & 1 & 0 & 0 & 0 \\ 0 & -0.28 & 9.81 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0.22 \\ 0 & 0 & 0 & 0 & -8.33 \end{bmatrix}$$

$$B_u = [0 \ 0 \ 0 \ 0 \ 664.3]^T,$$

$$B_d = [0 \ 1 \ 0 \ -6.72 \ 0]^T. \quad (3.22)$$

C , (20).

X- : A (3.22)

$$a_2 = -g = -9.81. \quad (3.22).$$

Z- :

$$A = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 0.0173 \\ 0 & 0 & -8.33 \end{bmatrix}, B_u = \begin{bmatrix} 0 \\ 0 \\ 664.3 \end{bmatrix}, C = \begin{bmatrix} 1 \\ 0 \end{bmatrix} \quad (3.23)$$

- :

$$A = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 0.0068 \\ 0 & 0 & -8.33 \end{bmatrix}.$$

, (3.23).

3.2.

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 H_{∞}
 SOF- , LQR.
 Y-
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 :

$$\frac{d}{dt}x(t) = A_x x(t) + B_u u(t) + B_d d(t),$$

$$v(t) = C_x x(t),$$

$$\xi(t) = \begin{bmatrix} \sqrt{Q} & 0 \\ 0 & \bar{R} \end{bmatrix} \begin{bmatrix} x(t) \\ u(t) \end{bmatrix} \quad (3.24)$$

$$Q \quad R \quad (3.24)$$

LQR:

$$J = \int_0^{\infty} z(t)^2 dt = \int_0^{\infty} (x^T Q + u^T R) dt.$$

L_2

$$\frac{\int_0^{\infty} z(t)^2 dt}{\int_0^{\infty} d(t)^2 dt} = \frac{\int_0^{\infty} (x^T Q + u^T R) dt}{\int_0^{\infty} (d^T d) dt} \gamma^2. \quad (3.25)$$

d

H_{∞} -

SOF-

SOF K

(3.24),

L_2

(3.25).

L ,

$$P = P^T \geq 0:$$

$$P + A^T P + Q + \frac{1}{\gamma^2} P B_d B_d^T P - P B_u R^{-1} B_u^T P + L^T R^{-1} L = 0 \quad (3.26)$$

γ ,

$$\|W_{\xi}(s)\|_{\infty} = \gamma, \quad (3.27)$$

$$\gamma \quad \gamma \quad \|W_\xi(s)\|_\infty - H_\infty \quad d$$

SOF

$$K = R^{-1}(B_d^T P + L)C^T(C \cdot C^T)^{-1}. \quad (3.28)$$

X- Y- Z-
SOF PD-

$$K_z = K_p p_z + K_d p_z, K_\psi = K_p \psi + K_d \psi. \quad (3.29)$$

$K_p \quad K_d$

(2,5)

SOF:

$$K_z = 10p_z + 7p_z, K_\psi = 15\psi + 10\psi.$$

H_∞

SOF-

Y- X-

:

$$Q = d \quad g\{10^3, 1.5 \cdot 10^3, 4 \cdot 10^3, 10^6\}, R = 2.5 \cdot 10^3.$$

$$\gamma = 0.1.$$

SOF:

$$K_y = [-0.63, 1.46, 27.39, 20.73],$$

$$K_x = [0.63, -1.46, -27.39, -20.73].$$

SOF

L_2

$$\|W_\xi(s)\|_\infty : \|W_\xi(s)\|_2 = 0.0856$$

$$\|W_\xi(s)\|_\infty = 0.1291.$$

$$\gamma = 0.1.$$

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"QGroundControl" (.3.3)

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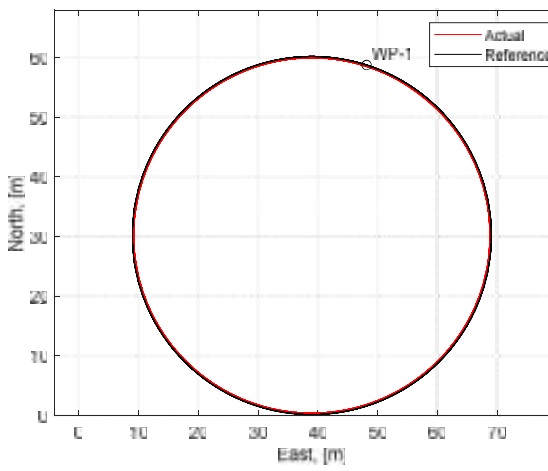
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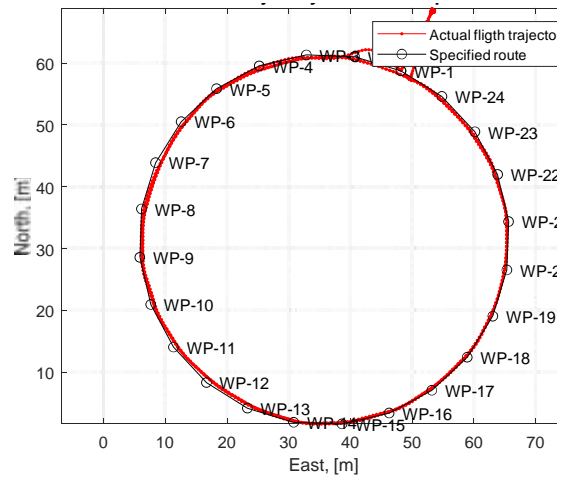


. 3.3

"QGroundControl"



(a)

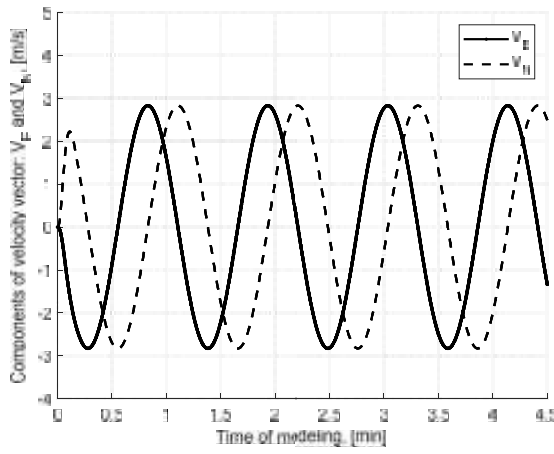


(b)

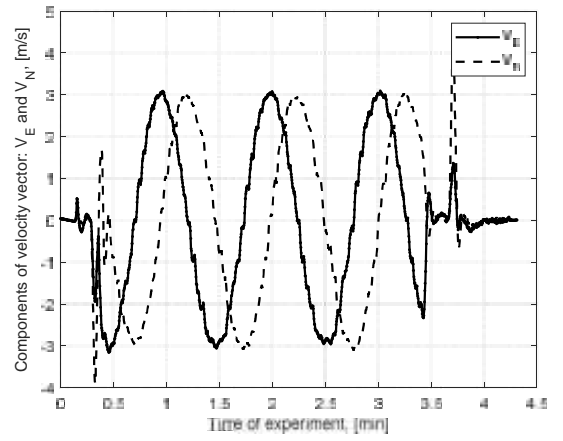
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(a)

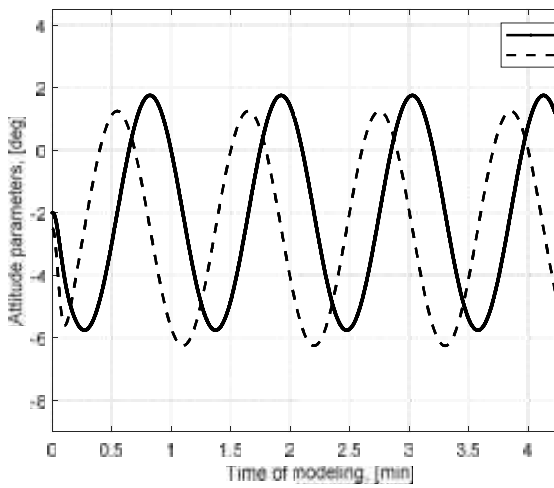


(b)

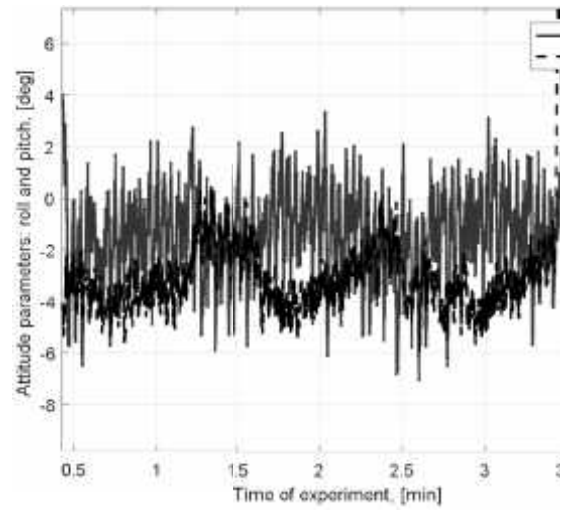
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(a)

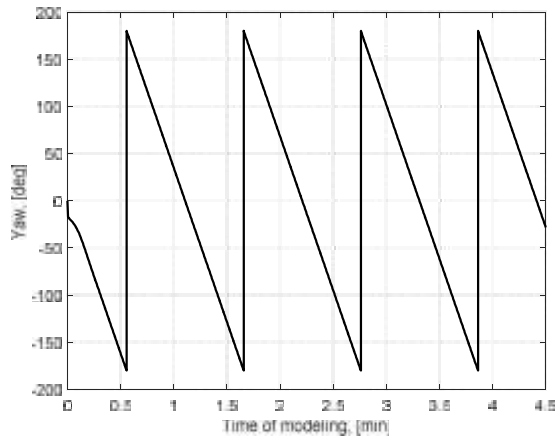


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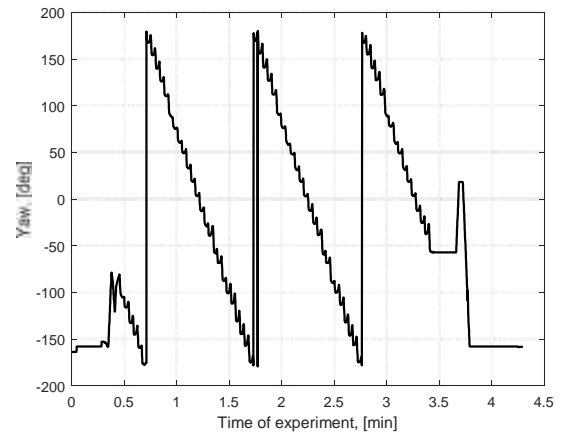
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$$: H = h +$$

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$$h = 0,8 -$$

$$h = 1 -$$

$$, H = 3 + 0,8 + 1 = 4,8$$

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$$S = nah = 31,5 = 6,75 \quad 2$$

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