

Squared error

$$\varepsilon^2 = S^2 - 2S\mathbf{w}^T + \mathbf{w}^T \mathbf{u}_{\text{сн}}^* \mathbf{u}_{\text{сн}}^T \mathbf{w}$$

Finding the expectation of ε^2 , we obtain an expression for the mean square error

$$E[\varepsilon^2] = S^2 + \mathbf{w}^T \mathbf{R}_{\text{сн}} \mathbf{w} - 2\mathbf{w}^T \mathbf{r}_{\text{сн},c}, \quad (2)$$

where $\mathbf{r}_{\text{сн},c} = \overline{\mathbf{u}_{\text{сн}}^* S}$; E – average.

Correlation matrix $\mathbf{R}_{\text{сн}}$ is the sum of the correlation matrix $\mathbf{R}_{\text{п}}$ interference and signal $\mathbf{R}_{\text{с}}$, $\mathbf{R}_{\text{сн}} = \mathbf{R}_{\text{п}} + \mathbf{R}_{\text{с}}$. From fig. 1 shows that the formation of the error signal $\mathbf{R}_{\text{сн}} = \mathbf{R}_{\text{п}} + \mathbf{R}_{\text{с}} - \mathbf{R}_{\text{с}} = \mathbf{R}_{\text{п}}$.

Vector $\mathbf{r}_{\text{сн},c}$ in the expression (2) is a correlation vector voltage $U_{\text{сн}i}^*$ i S ($i=1,2, \dots, N$), at $S_i^*=0$, ie the reference signal is missing

$$\mathbf{r}_{\text{сн},c}^T = [\overline{\mathbf{u}_{\text{сн}1}^*} \overline{\mathbf{u}_{\text{сн}2}^*} \dots \overline{\mathbf{u}_{\text{сн}N}^*}],$$

where $U_{\text{сн}i}^* = U_{\text{и}i}^*$.

Otherwise

$$\mathbf{r}_{\text{сн},c}^T = \mathbf{r}_{\text{п}}^T$$

Then the expression (2) takes the form

$$E[\varepsilon^2] = S^2 + \mathbf{w}^T \mathbf{R}_{\text{п}} \mathbf{w} - 2\mathbf{w}^T \mathbf{r}_{\text{п}}, \quad (3)$$

Optimization of the expression (3) in its minimization by selecting weighting coefficients vector \mathbf{w} . Since the mean square error (3) quadratic function of the vector \mathbf{w} it has only minimum which can be found by differentiating (3) and equating to zero the derivative

$$dE[\varepsilon^2]/d\mathbf{w} = 0. \text{ Так как } dE[\varepsilon^2]/d\mathbf{w} = 2\mathbf{R}_{\text{п}}\mathbf{w} - 2\mathbf{r}_{\text{п}} \quad (4)$$

vector weights will be determined by the expression

$$\mathbf{w} = \mathbf{R}_{\text{п}}^{-1} \mathbf{r}_{\text{п}}, \quad (5)$$

Expression (5) corresponds to the expression Wiener-Hopf for calculating the weights in an adaptive antenna array.

The scheme in fig. 1 to satisfy the minimum mean square error. Here are the results of mathematical modeling. The simulation results (fig. 2, fig. 3) for interference azimuth 241° , elevation 28° , matrix AAA 4×4 , $dx, dy = 0.25$, variance of noise - 1, phase shift interference 0° .

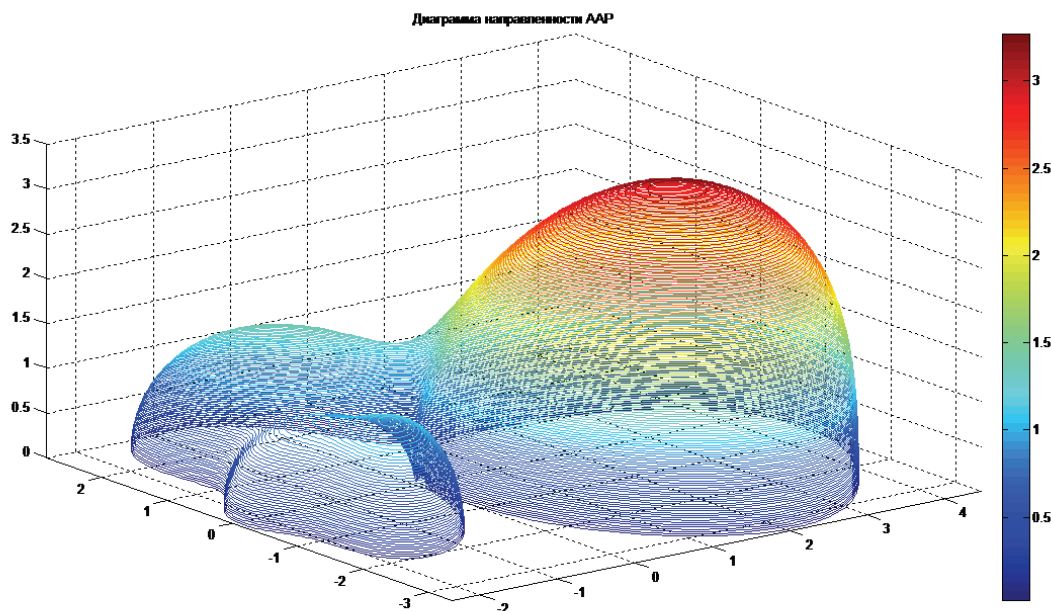


Figure 2

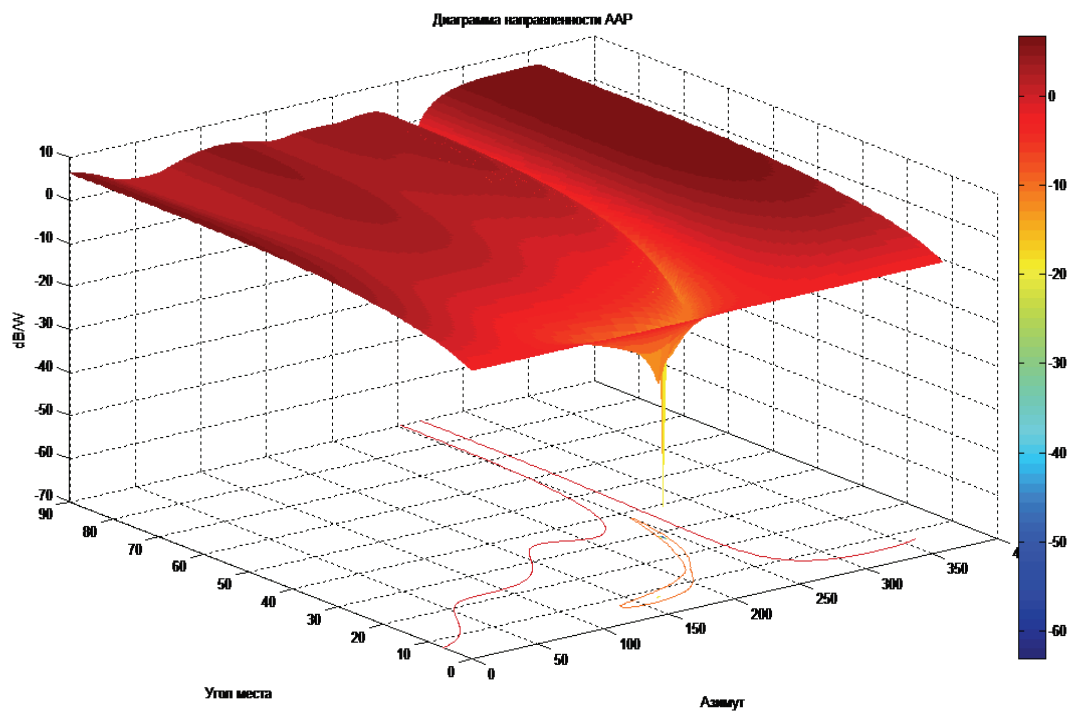


Figure 3

Conclusions

The proposed method allows to calculate the weights to control the pattern AAA GPS systems without knowing the useful signal. These results suggest that the quality of the noise reduction is not worse given in [3].

References

1. Адаптивная компенсация помех в каналах связи / Ю. В. Лосев, А. Г. Бердников, Э. Ш Гойхман, Б. Д. Сизов – М.: Радио и связь, 1988. – 208 с.
2. Цифровое формирование диаграммы направленности в фазированных антенных решетках / Л. Н. Григорьев – М.: Радиотехника, 2010. – 144 с.
3. Адаптивные антенные решетки: Введение в теорию / Р. А. Монзинго, Т. У. Миллер – М.: Радио и связь, 1988. – 448 с.